

# Market Power, Innovation, and the Green Transition

Rik Rozendaal

Leiden University

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# Introduction

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- | Winners and losers within industries

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*How does market power affect the transition from a dirty to a clean economy?*

# Contribution and results

## Contribution to the literature:

- | Empirical evidence on market power and the direction of innovation: cannot be explained by current theories
- | A theoretical model that incorporates empirical findings and explores the relevance for climate policy

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## Preview of findings:

- | Data: market leaders are, on average, more invested in dirty technologies than their direct competitors
- | Theory: climate policy can lead to a strategic increase in dirty innovation by some firms because of the "escape competition effect"
- | Calibration: ambitious climate policy leads to a (mostly clean) research boom and lower aggregate markups along the green transition

# Literature

## | Directed technical change and the environment

- | Theory: direction of innovation responds to relative prices, market sizes, and stocks of knowledge (path dependence)

Smulders and de Nooij (2003); Acemoglu et al. (2012, 2016), Aghion et al. (2024)

- | Empirics: DTC mechanisms and policies affect innovation

Jaffe and Palmer (1997); Newell et al. (1999); Popp (2002); Linn (2008); Noailly and Smeets (2015); Aghion et al. (2016); Calel and Dechezleprêtre (2016); Rozendaal and Vollebergh (2024)

- | Porter hypothesis: environmental regulation and competitiveness

Porter (1990); Porter and van der Linde (1995)



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## | Market power and innovation

- | Growth through creative destruction: technology ladders

Schumpeter (1942); Aghion and Howitt (1992); Grossman and Helpman (1991)

- | Competition ( ) innovation; strategic interaction

Blundell et al. (1995); Aghion et al. (2005); Akcigit and Ates (2023)

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Establish the following facts:

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Evidence suggests that market leaders are more invested in dirty technologies than their competitors

- | More difficult to make them switch to clean

Data from Orbis IP and Historical

- | 130 million patent applications; 1.4 million inventions
- | Classified as clean, dirty, neutral following Jee and Srivastav (2023)
- | Mostly energy, manufacturing, transport technologies
- | Link between firms' patents and balance sheets

Data

Shares clean dirty

Totals clean dirty

Types of clean technologies

Types of dirty technologies

Gray as a share of dirty

Patents by applicant country

Patents by applicant sector

## Path dependence in innovation

Knowledge stocks:  $K_{it}^T = P_{it}^T + (1 - \delta)K_{it-1}^T$ , with  $T \in \{C, D\}$

Innovation gap $_{it} = \sinh^{-1}(P_{it}^C) - \sinh^{-1}(P_{it}^D)$

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The direction of innovation is path dependent:

- | Clean patenting depends positively on  $K^C$  and negatively on  $K^D$   
Regression table
- | Vice versa for dirty patenting
- | In line with the literature

# Which firms are most invested in dirty technologies?

I define:

- | Leaders: top 10 firms in terms of revenue in country-sector-year
- | Laggards: firms in ranks 11-20



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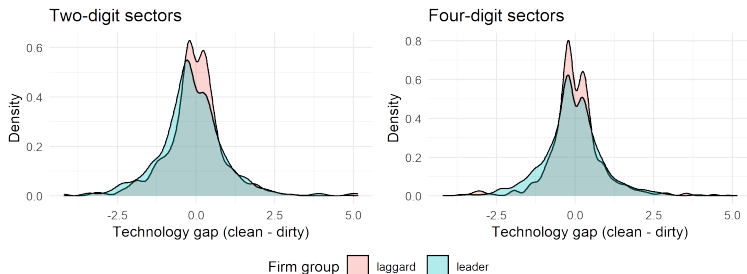


Figure: Distribution of the technology gap for leaders and laggards in 2018

# Which firms are most invested in dirty technologies?

Within a country-industry-year, technology gap correlates negatively with:

- | Firm size, profitability and age [Regression table](#)
- | Being a market leader [Regression table](#)

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So, firms with more market power tend to be dirtier.

Suggests that:

- | Large firms need a stronger incentive to switch to clean than smaller firms
- | Climate policy can affect market power

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Suggests that:

- | Large firms need a stronger incentive to switch to clean than smaller firms
- | Climate policy can affect market power

Cannot be explained by the current literature, so let's incorporate these findings in a model

- | What does this mean for climate policy?

# Model overview

## Continuous time endogenous growth model:

- | Representative consumer
- | Final good consists of a continuum of intermediates
- | Exponential-quadratic damages from climate change (Nordhaus and Moat, 2017)
- | Temperature linear in historical emissions (Dietz and Venmans, 2019)

Details

# Model overview

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### Details

## Each intermediate input sector has:

- | Two firms that compete on prices (limit pricing) (Akcigit and Ates, 2023)
- | Good produced using either a clean or a dirty technology
- | Stepwise innovation in clean and dirty
- | Knowledge diffusion

Production

Innovation

Technology gaps

Static decision

Dynamic decision

# Technology gaps

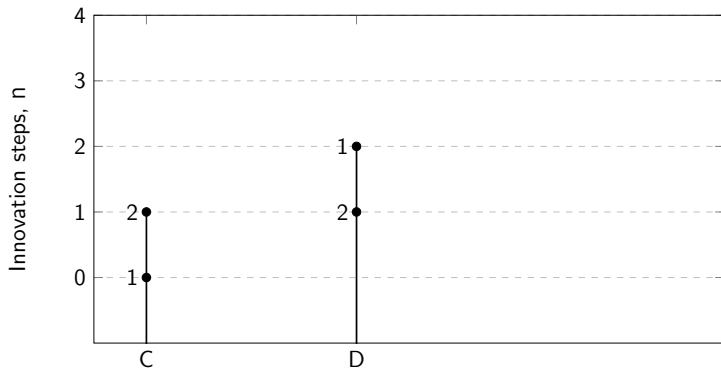


Figure: Own, clean and dirty technology gaps

# Technology gaps

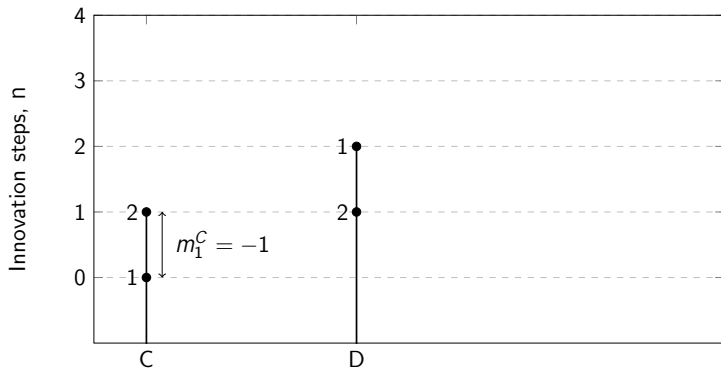


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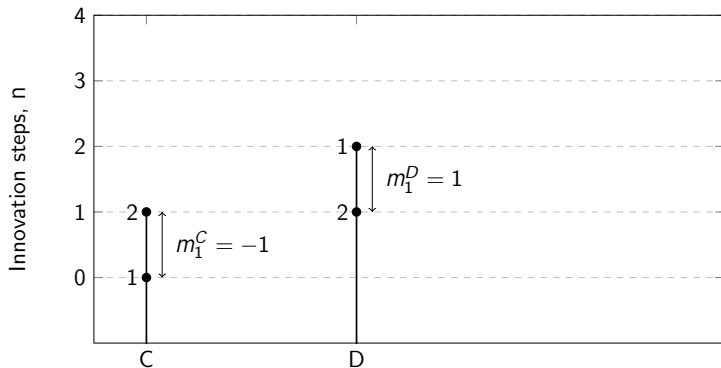


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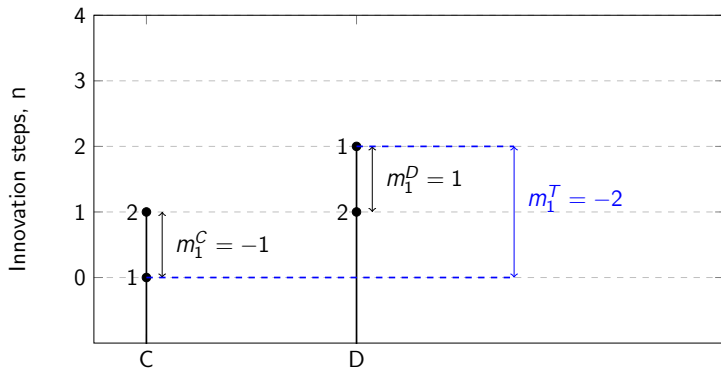


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# The effect of a tax

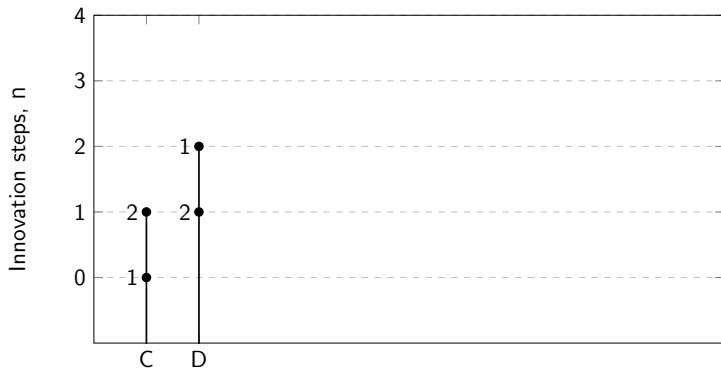


Figure: A carbon tax affects the effective technology gap

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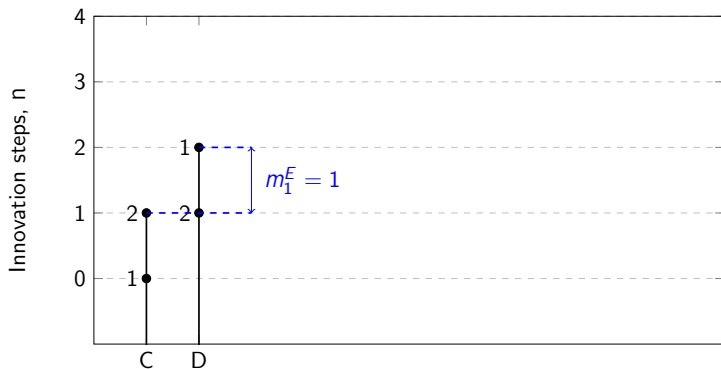


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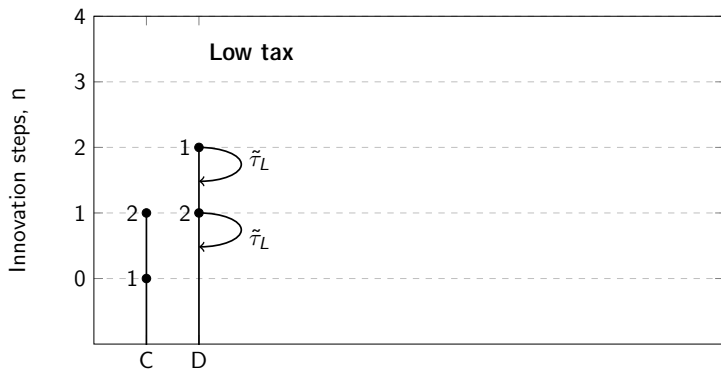


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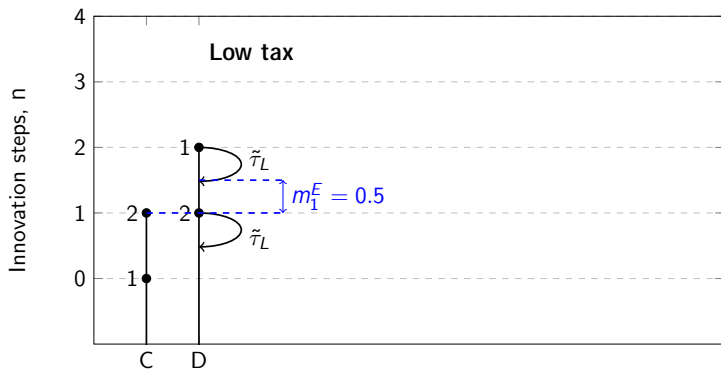


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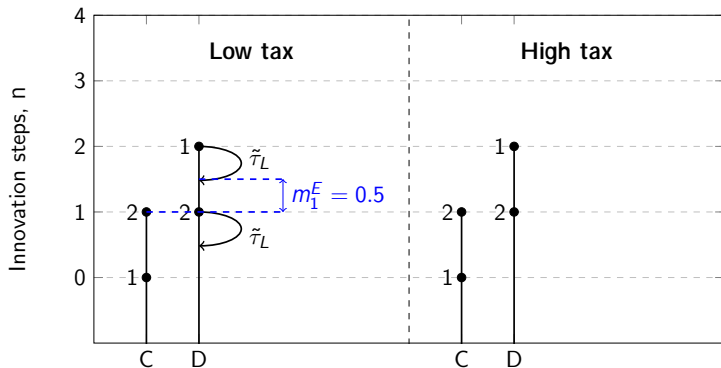


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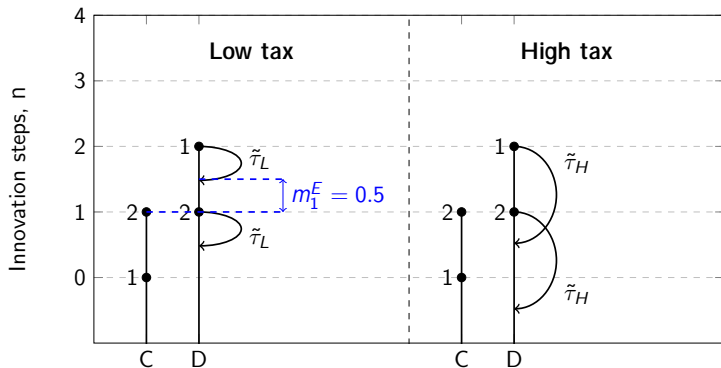


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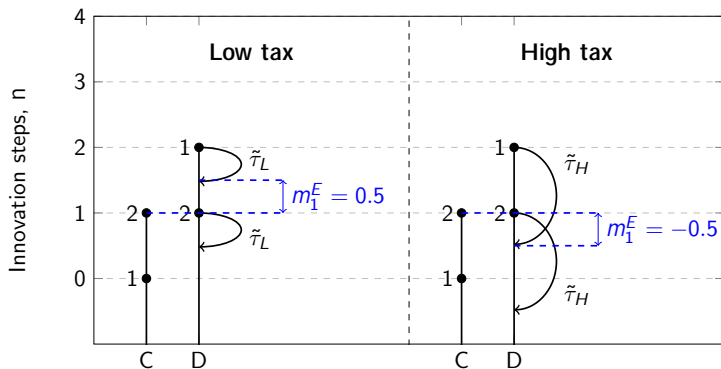


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# Stepwise innovation

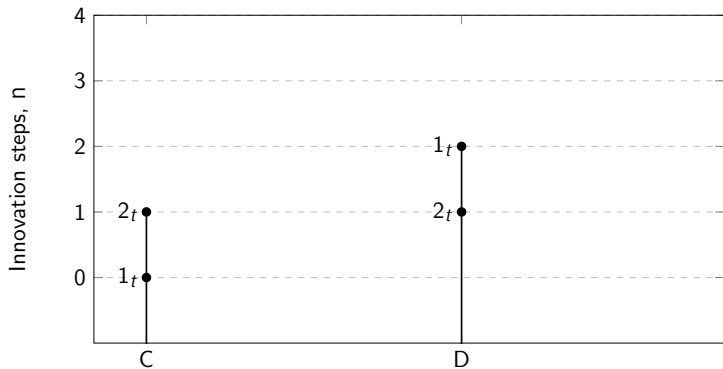


Figure: Clean and dirty innovation

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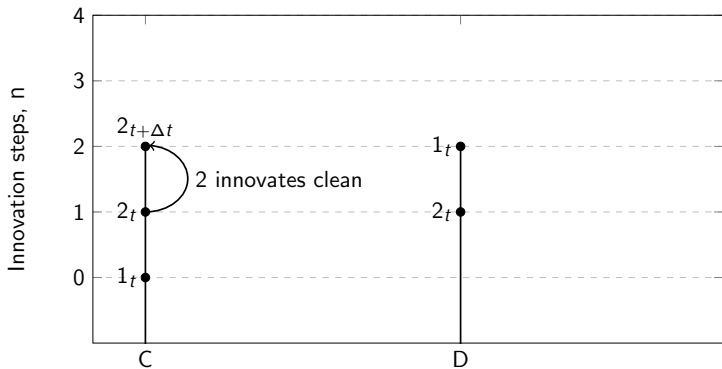


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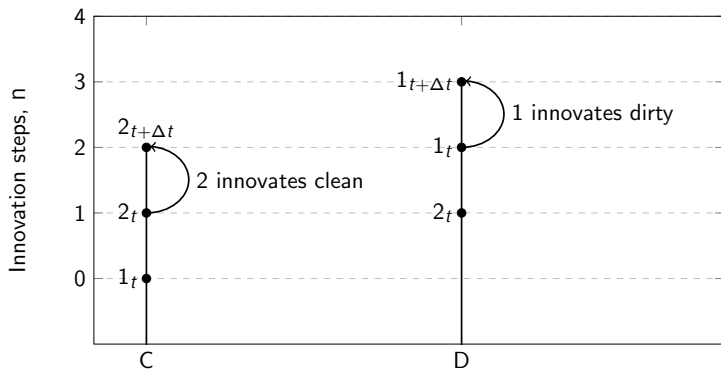


Figure: Clean and dirty innovation

## A partial equilibrium result

The increase or introduction of a carbon tax in a single sector can increase a firm's dirty innovation efforts:

- | Tax decreases effective technology gap
- | Increased competition and innovation due to escape competition effect (Aghion et al., 2005)

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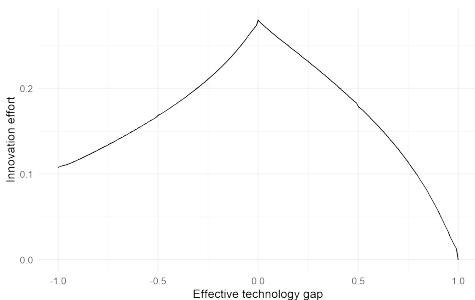


Figure: Innovation efforts for different technology gaps

# Calibration

Solve for the general equilibrium in closed form

General equilibrium

BGP

$\mu_{mt}$  by group

$w_t, \omega_t, Y_t, E_t, R_t^C, R_t^D$

Law of motion  $Q_t, \psi_{klmt}, \mu_{mt}$

Calibrate model to world economy in 2010s

- | External parameters from the literature
- | Initial conditions based on patent and financial data
- | Internal calibration of remaining parameters following Akcigit and Ates (2023)

External parameters

Initial conditions

Calibration results and model fit

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Initial conditions

Calibration results and model fit

Two quantitative exercises:

- | Simulate BGP: business as usual
- | Transition after large carbon tax increase in 2024 (Paris goal in 2100)



# Balanced growth path

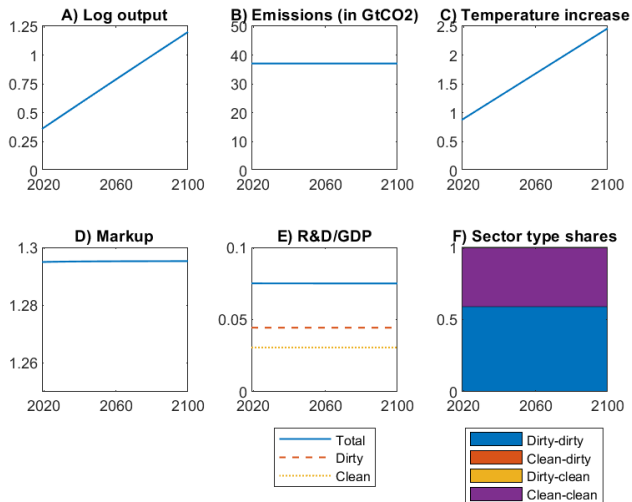


Figure: Balanced growth path simulated forward

# The effects of a carbon tax

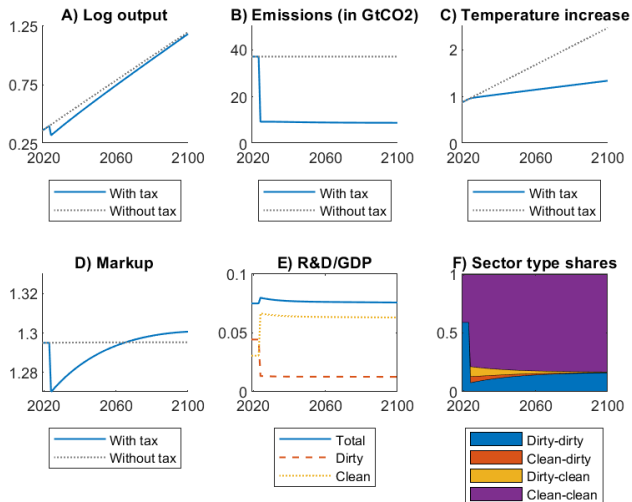


Figure: Transition after a large carbon tax increase in 2024

# Conclusions

- | Data suggests that market leaders are more invested in dirty technologies than their competitors
- | Model shows how this impacts the green transition
  - | Some firms increase their dirty innovation
  - | Increased innovation and competition along the transition
- | Suggests that transition may be less costly than anticipated
  - | But it may not be so simple (overinvestment in R&D)
- | Considering the strategic incentives for large incumbents is key for a successful green transition

Thanks!

r.l.rozendaal@law.leidenuniv.nl

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# Data

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  - | 1978-2018
  - | Counts of triadic patent families to avoid double counting and low quality inventions
  - | Classified as clean, dirty, neutral following Jee and Srivastav (2023)
  - | Mostly energy, manufacturing, transport technologies
  - | Link to financial data

## Orbis Historical

- | Balance sheet and other financial data for millions of firms
  - | 2010-2018
  - | Mostly developed countries
  - | Revenue, employees, profit, age, sector
  - | Issues with coverage and representativeness
  - | Focus on matched firms and top firms per sector

# Clean and dirty patenting

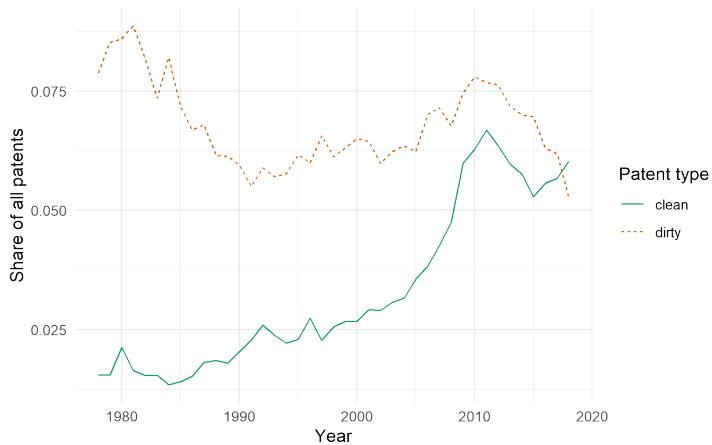
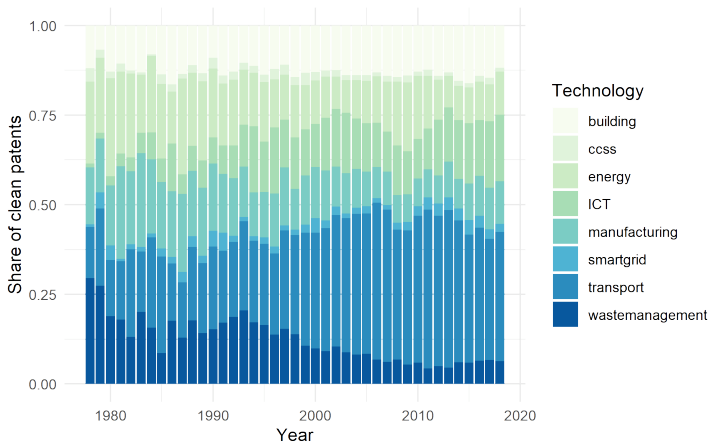


Figure: Share of clean and dirty patents over time

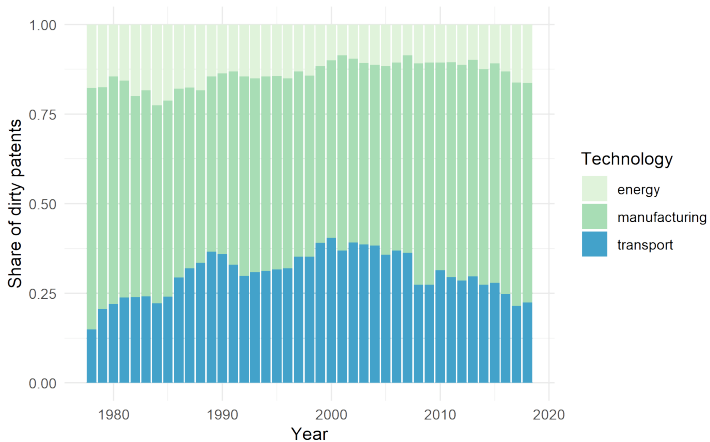


Figure: Different types of clean technologies



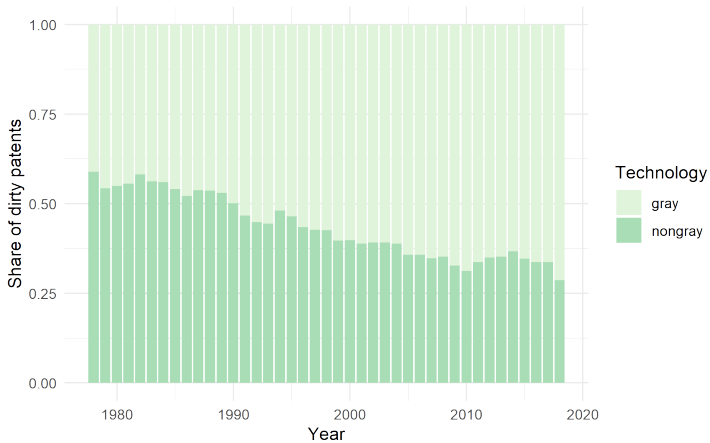
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Figure: Different types of clean technologies



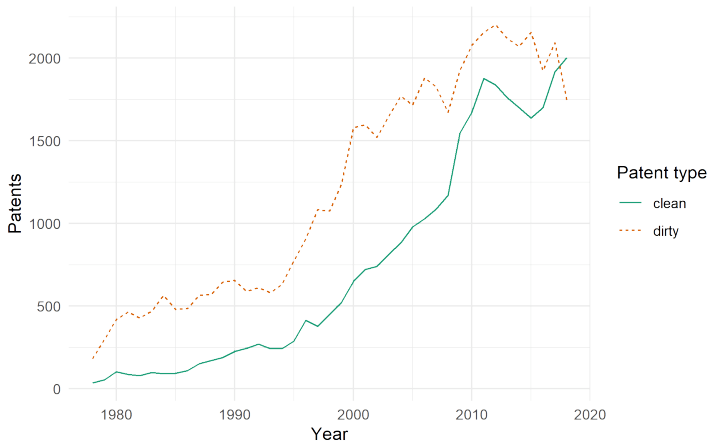
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Figure: Share of gray patents among dirty patents



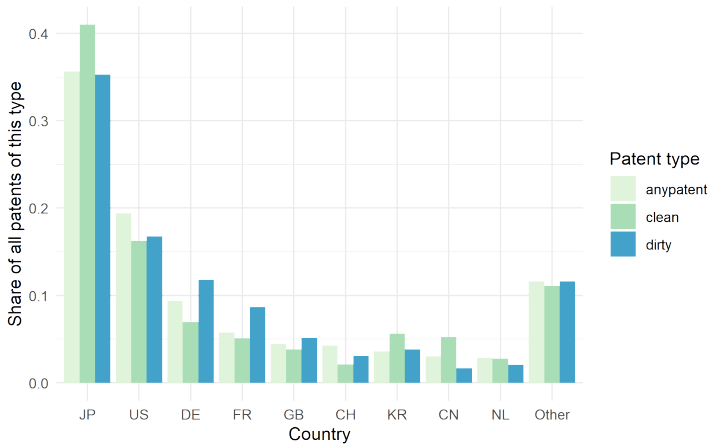
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Figure: Total clean and dirty patents over time



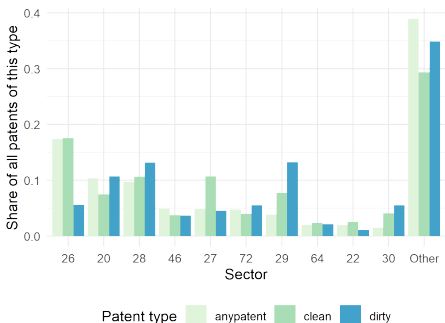
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Figure: Patents by applicant country



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Figure: Patents by applicant sector



Sectors are classified using the NACE Rev. 2 classification. The sectors in the figure are the following. 26: Manufacture of computer, electronic and optical products; 20: Manufacture of chemicals and chemical products; 28: Manufacture of machinery and equipment n.e.c.; 46: Wholesale trade, except of motor vehicles and motorcycles; 27: Manufacture of electrical equipment; 72: Scientific research and development; 29: Manufacture of motor vehicles, trailers and semi-trailers; 64: Financial service activities, except insurance and pension funding; 22: Manufacture of rubber and plastic products; 30: Manufacture of other transport equipment.

Table: Path dependence in innovation

	(1)	(2)	(3)	(4)
	Clean	Dirty	Innovation gap (clean-dirty)	
Log $K^C$	0.525	-0.196	0.020	
	(0.021)	(0.013)	(0.003)	
Log $K^D$	-0.032	0.879	-0.041	
	(0.021)	(0.017)	(0.002)	
Technology gap (clean-dirty)				0.241
				(0.007)
Estimator	Poisson	Poisson	OLS	OLS
(Pseudo) $R^2$	0.55	0.58	0.12	0.24
Observations	6,624,288	6,624,288	4,215,743	4,112,920

Notes: All independent variables are first lags. OLS regressions include country-sector-year fixed effects (sectors defined at the four-digit level). Further controls in columns 1 through 3 are the stock of patents in any category and dummies that are 1 if the stock variables equal zero (one dummy for each stock). Further controls in column 4 are the stock of patents in any category, a dummy that is 1 if the stock of patents is zero, and a dummy that is 1 if the technology gap is zero. Standard errors are clustered at the firm level. The sample covers the years 1978-2018.

**Table:** Technology gaps and market power

	(1)	(2)	(3)	(4)
	Technology gap (clean-dirty)			
Log revenue	-0.005 (0.002)		-0.004 (0.002)	
Log employment	0.001 (0.002)		-0.001 (0.002)	
Profit margin	0.000 (0.000)		0.000 (0.000)	
Log age	0.002 (0.002)		0.003 (0.003)	
Leader		-0.045 (0.011)		-0.023 (0.006)
Laggard		-0.008 (0.008)		-0.003 (0.005)
Sectors (for leader and f.e.)	Two-digit	Two-digit	Four-digit	Four-digit
R <sup>2</sup>	0.06	0.05	0.16	0.13
Observations	223,088	401,587	208,462	380,164

Notes: All regressions are OLS with country-sector-year fixed effects. Column 2 and 4 define leaders as the top 10 firms in their two-digit and four-digit sector in terms of revenue, respectively. Fixed effects are defined at the two-digit sector in columns 1 and 2 and at the four-digit level in columns 3 and 4. All independent variables are contemporaneous values. Standard errors are clustered at the firm level. The sample covers the years 2010-2018.



**Table:** Heterogeneity in technology gaps (four-digit sectors)

	(1)	(2)	(3)	(4)
	Technology gap (clean-dirty)			
Log revenue	-0.003 (0.001)			
Log employment		-0.004 (0.001)		
Profit margin			-0.000 (0.000)	
Log age				-0.004 (0.001)
R <sup>2</sup>	0.13	0.14	0.15	0.10
Observations	372,506	342,421	262,588	835,951

Notes: All regressions are OLS with country-sector-year fixed effects. Fixed effects are defined at the four-digit sector. All independent variables are contemporaneous values. Standard errors are clustered at the firm level. The sample covers the years 2010-2018.

# Preferences, final good, global warming

**Representative consumer:**  $U_t = \int_{s=t}^1 \exp(-\rho(s-t)) \ln(C_s) ds,$

Labor  $L$  is supplied inelastically to production or R&D,  $L_t = 1$

**Final good:**  $\ln Y_t = \frac{\gamma}{2} T_t^2 + \int_0^1 \ln y_{jt} dj,$

with damages from global warming  $T$ , scaled by

**Global warming:**  $T_t = \theta(S_t - T_t),$

with  $\theta$  the linear effect of cumulative emissions  $S_t = \int_0^t E_s ds$  on temperature and  $\theta$  a delay parameter (Dietz and Venmans, 2019)

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# Intermediate good sectors

**Firms:** each sector  $j$  consists of two firms,  $i$  and  $i'$ , which compete on prices

**Production:**  $y_{ijt} = y_{ijt}^C + y_{ijt}^D = q_{ijt}^C l_{ijt}^C + q_{ijt}^D \min \left\{ l_{ijt}^D; \frac{e_{ijt}}{\kappa} \right\}$ ;

with  $q$  productivity,  $l$  labor,  $e$  emissions,  $C$  clean,  $D$  dirty

**Total costs:**  $TC_{it} = w_t l_{it}^C + w_t l_{it}^D + \frac{E}{t} e_{it} = w_t l_{it}^C + w_t (1 + \tau_t) l_{it}^D$ ;

with  $w$  wage and  $\frac{E}{t} = \tau_t w_t$  carbon price relative to labor

**Marginal costs:**  $MC_{it} = \min \{ MC_{it}^C; MC_{it}^D \} = \min \left\{ \frac{w_t}{q_{it}^C}; \frac{w_t(1+\kappa\tau_t)}{q_{it}^D} \right\}$

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# Innovation

**Innovation steps:** in case of a successful innovation,  $q_{i(t+\Delta t)}^F = q_{it}^F$ ,

where  $F \in \{C, D, G\}$

So,  $q_{it}^F = n_{it}^F$ , where  $n_{it}^F$  is the number of innovation steps that firm  $i$  has taken for technology  $F$  (assuming  $q_{i0}^F = 1$ )

**Innovation costs:**  $R_{it} = \frac{x_{it}^\beta}{\beta} w_t$ ,

where  $x$  is the innovation arrival rate

**Knowledge diffusion:** catch up with leader with exogenous arrival rate (technology gap becomes 0)

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# Technology gaps

Own, clean, dirty:

Own technology gap:  $m_{it}^T = n_{it}^C \quad n_{it}^D$

Clean technology gap:  $m_{it}^C = n_{it}^C \quad n_{it}^D$

Dirty technology gap:  $m_{it}^D = n_{it}^C \quad n_{it}^D$

Firm  $i$  uses clean to produce  $i$   $m_{it}^T + \gamma > 0$  with  $\gamma = \frac{\ln(1+\kappa\tau_t)}{\ln(\lambda)}$

Effective technology gap:

$$m^E(m_{it}^C; m_{it}^D; m_{it}^T; \gamma) = \begin{cases} m_{it}^C & \text{if } m_{it}^T + \gamma > 0; \quad m_{it}^D + \gamma > 0 \\ m_{it}^D + m_{it}^T + \gamma & \text{if } m_{it}^T + \gamma > 0; \quad m_{it}^D + \gamma < 0 \\ m_{it}^C \quad m_{it}^T + \gamma & \text{if } m_{it}^T + \gamma < 0; \quad m_{it}^D + \gamma > 0 \\ m_{it}^D & \text{if } m_{it}^T + \gamma < 0; \quad m_{it}^D + \gamma < 0 \end{cases}$$

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# Static competition

**Demand:**  $y_{jt} = \frac{Y_t}{p_{jt}}$

**Bertrand competition:** limit pricing:

$$p_{jt} = \begin{cases} MC_{it} & \text{if } m_{it}^E > 0 \\ MC_{it} & \text{if } m_{it}^E = 0 \end{cases}$$

Only market leader makes a profit:

$$m_{it}^E = \begin{cases} (p_{jt} - MC_{it})y_{it} = \left(1 - \frac{1}{\lambda \frac{m_{it}^E}{Y_t}}\right) Y_t & \text{if } m_{it}^E > 0 \\ 0 & \text{if } m_{it}^E = 0 \end{cases}$$

Also gives each firm's output, labor demand and emissions

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# Innovation decision

## Direction:

- | Currently clean firms ( $m_{it}^T + \tau_t > 0$ ) innovate in clean technology
- | Currently dirty firms ( $m_{it}^T + \tau_t < 0$ ) innovate in dirty technology

**Intensity:** maximize NPV of profits given current effective technology gap  $m$

A normalized value function for each possible  $m$ :  $v_{mt} = V_{mt} = Y_t$

For leaders ( $m > 0$ ):

$$v_{mt} = \max_{x_{mt}} \left\{ 1 - \frac{1}{m} \left[ \frac{x_{mt}^\beta}{m} Y_t + x_{mt} [V_{m+1,t} - v_{mt}] + x_{mt} [V_{m-1,t} - v_{mt}] + [V_{0,t} - v_{mt}] \right] \right\}$$

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# General equilibrium

Define:

- | Maximum effective gap  $\bar{m}$
- | Maximum distance between clean and dirty  $\bar{m}^T$
- | Aggregate productivity index  $Q_t = \exp\left(\int_0^1 \ln(q_{Ljt}) dj\right)$
- | Gap size distribution to keep track of technology gaps (3 state variables per sector):  $klmt = \int_0^1 1\{m_{Ljt}^T = k \wedge m_{Fjt}^T = l \wedge m_{Ljt}^E = m\} dj$
- | Effective gap size distribution  $m_t = \sum_{k=0}^{\bar{m}^T} \bar{m}^T \sum_{l=0}^{\bar{m}^T} \bar{m}^T klmt$  (by group)

Gives closed form solutions for  $\omega_t, E_t, W_t, Y_t, R_t^C, R_t^D$

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# Balanced growth

Along the balanced growth path...

- | The effective gap distribution is constant
- | The gap between clean and dirty within sectors is growing
- | There are no "mixed sectors" due to knowledge diffusion
- | TFP growth is constant (but, if  $E_t > 0$ , output growth is not)

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$$DD_{mt} = \sum_{k \in 2M_t^D} \sum_{l \in 2M_t^D} klmt ;$$

$$CD_{mt} = \sum_{k \in 2M_t^C} \sum_{l \in 2M_t^D} klmt ;$$

$$DC_{mt} = \sum_{k \in 2M_t^D} \sum_{l \in 2M_t^C} klmt ;$$

$$CC_{mt} = \sum_{k \in 2M_t^C} \sum_{l \in 2M_t^C} klmt ;$$

$$1t = \sum_{m \in 2M_t} DD_{mt} ;$$

$$2t = 1 + \sum_{m \in 2M_t} CD_{mt} ;$$

$$3t = 1 - \sum_{m \in 2M_t} CC_{mt}$$

$$I_t = \left( \sum_{k \in M_t} \frac{DD_{kt} + \frac{CD_{kt}}{k} + \frac{DC_{kt} + \frac{CC_{kt}}{k}}}{(1 + \frac{\cdot}{t})^k} \right) \left( 1 + \sum_{k \in M_t} \mu_{kt} (X_{Ljt}^\beta + X_{Fjt}^\beta) \right)^{-1};$$

$$E_t = \frac{1}{I_t} \sum_{k \in M_t} \frac{DD_{kt}}{(1 + \frac{\cdot}{t})^k} + \frac{DC_{kt}}{k};$$

$$W_t = \frac{Q_t \sum_{k \in M_t} \mu_{kt}^k \exp\left(-\frac{\gamma}{2} T_t^2\right)}{(1 + \frac{\cdot}{t})^{\theta_{2t}}};$$

$$Y_t = \frac{W_t}{I_t};$$

$$G_t = \frac{1}{t} W_t E_t$$

$$R_t^C = \frac{W_t}{I_t} \sum_{k \in M_t} \left( \frac{CD_{kt}}{k} X_{kt}^\beta + \frac{DC_{kt}}{k} X_{kt}^\beta + \frac{CC_{kt}}{k} (X_{kt}^\beta + X_{kt}^\beta) \right);$$

$$R_t^D = \frac{W_t}{I_t} \sum_{k \in M_t} \left( \frac{DD_{kt}}{k} (X_{kt}^\beta + X_{kt}^\beta) + \frac{CD_{kt}}{k} X_{kt}^\beta + \frac{DC_{kt}}{k} X_{kt}^\beta \right);$$

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$$\ln(Q_{t+\Delta t}) - \ln(Q_t) = \left[ 2 \sum_{k \in M} \alpha_k X_{kt} + \sum_{p \in M} \beta_p (X_{pt} + (1 - \beta_p) X_{p,t-\Delta t}) \right. \\ \left. + \sum_{l \in M} \gamma_l (X_{l,t-\Delta t} + \beta_l X_{l,t-\Delta t}) \right] \ln(\cdot) + o(\Delta t)$$

$$\frac{\ln(Q_{k,l,m,t+\Delta t}) - \ln(Q_{k,l,m,t})}{\Delta t} = 1 \left\{ k + 1 + \gamma_t < 0 \right\} \alpha_{k+1,l,m} X_{m-1,t} \\ + 1 \left\{ k - 1 + \gamma_t > 0 \right\} \alpha_{k-1,l,m} X_{m-1,t} \\ + 1 \left\{ l + 1 + \gamma_t < 0 \right\} \alpha_{k,l+1,m+1,t} X_{m-1,t} \\ + 1 \left\{ l - 1 + \gamma_t > 0 \right\} \alpha_{k,l-1,m+1,t} X_{m-1,t} \\ + \alpha_{k,l,m,t} (X_{m,t} + X_{m,t-\Delta t}) + \frac{o(\Delta t)}{\Delta t}$$

$$\frac{FF_{m,t+\Delta t}}{\Delta t} - \frac{FF_{m,t}}{\Delta t} = \alpha_{m-1,t} X_{m-1,t} + \alpha_{m+1,t} X_{m-1,t} \\ + \alpha_{m,t} (X_{m,t} + X_{m,t-\Delta t}) + \frac{o(\Delta t)}{\Delta t}$$

# Calibration

Assume world economy is on a BGP in 2010s

Parameter	Value	Description	Source
$\rho$	1%	Rate of time preference	Acemoglu et al. (2016)
$\beta$	1/0.35	R&D cost curvature	Akcigit and Ates (2023)
$\gamma$	0.01	Climate damage elasticity	Dietz and Venmans (2019); Nordhaus and Moffat (2017)
$\zeta$	$0.00048 \times 1.1$	TCRE	Dietz and Venmans (2019); Matthews et al. (2009)
$\varepsilon$	0.5	Initial pulse-adjustment time-scale of the climate system	Dietz and Venmans (2019); Ricke and Caldeira (2014)

Table: Externally calibrated parameters

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# Calibration

## Initial conditions:

- | Initial share of clean and dirty firms
- | Emissions since 1850 to compute initial (2019) temperature
- | Initial gap distribution
  - | Define leaders as firm with highest absolute value of  $m^T$  (as defined in empirical section)
  - | Classify sectors as clean or dirty based on leader
  - | Laggard is second firm in terms of  $m^T$
  - | Fill in  $m=0, t=0$  using BGP effective gap distribution

# Calibration

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## Internal calibration procedure similar to Akcigit and Ates (2023):

- | For given  $f ; ; ; g$ , find BGP effective gap size distribution
- | Compute model moments
- | Minimize difference with data moments

# Calibration

Parameter	Value	Description
$\lambda$	1.0656	Innovation step size
$\delta$	0.0374	Diffusion arrival rate
$\alpha$	44.4299	R&D scaling parameter
$\kappa$	68.5578	Emission scaling parameter

Table: Internally calibrated parameters

Moment	Model	Data	Source
Average markup (2015)	1.2953	1.29	Díez et al. (2021)
Profit share (2018)	19%	19%	Eggertsson et al. (2021)
Productivity growth (avg. 2011-2019)	1.0738%	1.0738%	OECD
Emissions (2019, in GtCO <sub>2</sub> )	37.0826	37.0826	Friedlingstein et al. (2022)

Table: Model fit